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Integration of ART2 neural network and genetic K-means algorithm for analyzing Web browsing paths in electronic commerce

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Abstract

Neural networks and genetic algorithms are useful for clustering analysis in data mining. Artificial neural networks (ANNs) and genetic algorithms (GAs) have been applied in many areas with very promising results. Thus, this study uses adaptive resonance theory 2 (ART2) neural network to determine an initial solution, and then applies genetic K-means algorithm (GKA) to find the final solution for analyzing Web browsing paths in electronic commerce (EC). The proposed method is compared with ART2 followed by K-means.

In order to verify the proposed method, data from a Monte Carlo Simulation are used. The simulation results show that the ART2+GKA is significantly better than the ART2+K-means, both for mean within cluster variations and misclassification rate. A real-world problem, a recommendation agent system for a Web PDA company, is investigated. In this system, the browsing paths are used for clustering in order to analyze the browsing preferences of customers. These results also show that, based on the mean within-cluster variations, ART2+GKA is much more effective. © 2004 Elsevier B.V. All rights reserved.

Keywords: Clustering analysis; Data mining; ART2; Genetic K-means algorithm; Recommendation agent system

1. Introduction

Electronic commerce (EC) has developed rapidly in recent years. Because entering the Internet is not difficult and creating customer interaction is easy on the Internet, how to create long-term customer relationships is a critical factor for successful EC. The Institute for Information Industry (III) showed that there were over six million Internet users by the end of 2000, and it has increased dramatically. This results in more requirements for the analysis of network loading and more complexity of Web site design.

To help users in browsing Web contents is an important factor for designing a Web site. Thus, browsing behavior becomes an important index of effectiveness of a site. By analyzing the frequency of Web page clicks and by understanding the regular browsing paths, the structure of Web site can be improved and more popular Web pages can be provided to the customers, thereby increasing EC sales.

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Therefore, this research proposes a novel clustering analysis technique for data mining. It is employed to analyze the browsing paths and behaviors of EC customers in order to improve the development of Web sites and customer satisfaction. Clustering analysis is a common tool in multivariate analysis and has been applied widely in many areas. The purpose of clustering analysis is to determine the objects in the same cluster with similar characteristics. Furthermore, it determines when there is a significant difference between two different clusters. The applications of clustering analysis include social science, genetics, biology, business and education.

In addition to statistical methods, artificial neural networks (ANNs) have also been widely applied in such areas. The unsupervised neural network, which is able to cluster objects by learning from training samples, is especially useful. Genetic algorithms (GAs) also have this capability. Kuo et al. [11] have reported that very good solutions can be provided by using self-organizing feature maps (SOM) of neural networks to determine the number of clusters and the starting points, and then employing the K-means method to find the final solution. They also showed that K-means can be replaced by GA in order to get better results [11]. [10] Thus, this current study proposes using a modified two-stage clustering method, adaptive resonance theory 2 (ART2) neural network [3,4], followed by genetic K-means algorithm (GKA). The results are compared with those from ART2 followed by K-means.

In order to evaluate the performance of the two clustering analysis methods, both simulation and realworld data are employed. Both of sets of results indicate that the proposed method is better than ART2 followed by K-means. Then, the proposed method is applied to create a recommendation agent system for a PDA Web company, which can dramatically increase customer satisfaction.

The remainder of this paper is organized as follows. Section 2 introduces some necessary background, including applications of neural networks and genetic algorithms for clustering analysis. The proposed method is presented in Section 3, and Section 4 illustrates the simulation results. Section 5 shows the model evaluation results for a PDA Web company, and concluding remarks are made in Section 6.

2. Background

This section introduces some general background of data mining. In addition, applications of neural networks and genetic algorithms for clustering are also presented.

2.1. Data mining

Data mining is a popular research topic in EC, primarily used to extract usable information from huge data sets to more quickly make effective decisions. As one aspect of Knowledge Discovery in Databases (KDD) [20], it is able to find relevant patterns from huge data sets and to analyze usable information to aid in making choices. The concept of data mining is not simply regression analysis or a database management system (DBMS). To be a form of regression analysis, it should have a basic hypothesis and be able to process huge data set, whereas DBMS cannot analyze data to obtain more advanced information. Only data mining techniques, which combine statistics, data warehouse and machine learning, can act as a valuable tool for commercial purposes. Previously proposed methods for data mining can be categorized as follows: (1) association rules, (2) decision tree, (3) cluster analysis, (4) induction method, (5) statistic, (6) online analysis process or OLAP, (7) neural networks and (8) genetic algorithms [14]. This study will focus on third part, cluster analysis. Thus, applications of ANNs and genetic algorithms are summarized in the following two subsections. This study intends to realize the relationship between customer's browsing paths and preferences.

2.2. The application of ANNs in clustering analysis

An artificial neural network (ANN) is a system which has been derived through models of neurophysiology. In general, it consists of a collection of simple nonlinear computing elements whose inputs and outputs are linked to form the network.

The learning algorithms of ANNs can be divided either: supervised and unsupervised [5]. In supervised learning, the network has its output compared with a known answer and receives feedback about any errors. This is sometimes called learning with a teacher; the teacher tells the network what the correct answer is. For a supervised ANN, both inputs and outputs are necessary for training the network, so an unsupervised ANN requires only the inputs. This kind of network must itself discover patterns, features and correlations in the input data, and code for them in the output. The units and connections must thus display some degree of self-organization. The most widely applied unsupervised learning scheme is Kohonen's feature maps [8] and adaptive resonance theory [3,4].

A number of studies have successfully demonstrated the learning capability of ANNs and their applications for engineering, with very promising results. Proctor [21] indicated that ANN is an alternative expert system for the solution of marketing decision problems.

Venugopal and Bates [26] presented possible applications of self-organization feature maps with the marketing segmentation. Balakrishnan et al. [1] compared self-organizing feature maps with the K-means method. The result reveals that the K-means method has a higher rate of classification through the Monte Carlo algorithm [16,17]. Balakrishnan et al. [2] employed the frequency-sensitive competitive learning algorithm (FSCL) and the K-means method to cluster simulated data and real-world problem data, also presenting the combination of these two methods. Although neither the simulated nor the real-world problem data can determine which individual method is better, the combination of these two methods seems to provide better managerial explanation for the brand choice data. A modified two-stage method, which first uses the self-organizing feature maps to determine the number of clusters and the starting midpoint and employs the K-means method to find the final solution, was proposed by Kuo et al. [11] for market segmentation. The simulation results showed that the modified two-stage method is slightly more accurate than the conventional two-stage method (Ward's minimum variance method followed by the K-means method) with respect to the rate of misclassification. However, it is sometimes quite difficult to determine the number of clusters by observing the map, unless the topology maps clearly discriminate. However, another unsupervised ANN, Adaptive Resonance Theory (ART) neural network, does not have this disadvantage, so it can determine the actual number of clusters [19,25] without any further visual examination. It can also solve the problem of the difficulty of determining the number of clusters, like SOM neural network. Thus, the main advantages of ART2 are:

- 1. rapidly learning and adapting to a nonstable environment,
- 2. stability and plasticity,
- 3. unsupervised learning of preferences behavior that the target does not know initially, and
- 4. deciding the number of clusters exactly and automatically.

Adaptive resonance theory networks include ART1, which is applicable for binary data; and ART2 [3], which is used to deal with continuous data [4].

2.3. Applications of genetic algorithms in clustering analysis

Genetic algorithms (GAs), first developed by Holland [6], include several important phases like encoding and decoding, initial population, fitness function, reproduction, crossover and mutation. Genetic algorithms, which randomize search and simultaneously generate multiple solutions, provide better solutions than do general randomized search algorithms. Scott [22] applied genetic algorithms to propose a stable and efficient search technique, and subsequent results showed that it had a higher probability of finding the global optimum [24,27].

To date, there have already been some investigations on applying GA in clustering analysis. Selim and Ismail [23] proved that a conventional statistics method, like K-means algorithm, can easily find a local minimum, although it is necessary to develop a more robust method for clustering analysis. In Maulik and Bandyopadhyay's [15] experiments, the GA-clustering algorithm is superior to the K-means algorithm. Murthy and Chowdhury [18] proposed a GA-based method to solve the clustering problem and experiments on synthetic and real life data sets to evaluate the performance. The results showed that the GA-based method may improve the final output of K-means. Krishna and Murty [9] proposed a novel approach called Genetic K-means Algorithm (GKA) for clustering analysis, which defines a biased mutation operator specific to



Fig. 1. The process for evaluating two methods.

clustering called distance-based mutation. Using finite Markov chain theory, they proved that the GKA can converge to the global optimum, and in the simulations that GKA converged to the best-known optimum corresponding to the given data, concurring with the convergence result. Moreover, GKA searches faster than some of the other evolutionary algorithms used for clustering.

Kuo et al. [11] proposed a two-stage method which integrated both the SOM and K-means, with results indicating that the proposed method was much better than using only SOM or K-means. Then, they modified the GKA by Krishna and Murty and used SOM's solution as the initial solution for the modified GKA [12]. The results showed that this method was better than the previously published method, SOM+Kmeans. Kuo and Chung [10] also presented a method integrating of ART2 and genetic algorithm, which applied a different coding method.

3. Methodology

In this research, two clustering methods are proposed. In order to evaluate the efficiency of the two clustering methods, the Monte Carlo framework [16,17] is employed.

The data sets generated from the Monte Carlo method are used for evaluating the following methods:

- 1. A modified two-stage method uses the ART2 to determine the number of clusters and the initial points, and then employs the K-means algorithm to find the final solution. For a detailed discussion, refer to Kuo et al. [11]. This method referred to as ART2+K-means in this study.
- A novel two-stage method first uses the ART2 to determine the number of clusters, and then employs modified Genetic K-means Algorithm (GKA) to find the final solution. It is referred to as ART2+GKA.

In the following subsections, the related clustering methods and the Monte Carlo method are discussed in detail. Fig. 1 shows the process for evaluating these two methods.



Fig. 2. The architecture of ART2. Source: Ref. [4].

3.1. ART2 neural network

ART2 architectures are designed for processing analog as well as binary input patterns.

3.1.1. ART2 network architecture

Fig. 2 illustrates the architecture of the ART2 neural network, including F1 and F2 layers. There are six nodes in the F1 layer (W, X, U, V, P, Q). The input signal is processed by the F1 layer and then is passed from the bottom to top value $(b_{i,I})$. The result of the bottom to top value is an input signal of F2 layer. The nodes of F2 layer compete with each other to produce a winning unit. The winning unit returns the signal to the F1 layer. The match value is then calculated with top to bottom value (t_{Ji}) in the F1 layer and compared with the vigilance value. If the match value is greater than the vigilance value, then the weight of b_{iJ} and t_{Ji} is updated. Otherwise, the reset signal is sent to the F2 layer and the winning units inhibited. After inhibition, the other winning unit will be found in the F2 layer. If all of the F2 layer nodes are inhibited, the F2 layer will produce a new node and generate the initial corresponding weights to the new node.

3.1.2. The learning of the ART2 network F1 layer activation [13]:

$$u_i = \frac{v_i}{e + \parallel V \parallel} \tag{1}$$

 $w_i = s_i + a u_i \tag{2}$

$$p_i = u_i + dt_{Ji} \tag{3}$$

$$x_i = \frac{w_i}{e + \|W\|} \tag{4}$$

$$q_i = \frac{p_i}{e + \|P\|} \tag{5}$$

$$v_i = f(x_i) + bf(q_i). \tag{6}$$

where
$$f(x) = \begin{cases} x & \text{if } x \ge 0 \\ 0 & \text{if } x < 0 \end{cases}$$
.

Step 1: Initialize the parameters (a, b, c, d, e, α) and ρ and weights. In general, a=b=10, c=0.1 and d=0.9 to satisfy the equation:

$$\frac{cd}{1-d} \le 1 \tag{7}$$

where e=0; α is the learning rate; ρ is the vigilance with $0.7 < \rho < 1$; weight initializations are $t_{0i}=0$ and $b_{i0} = \frac{1}{(1-d)\sqrt{n}}$, in which *n* is the attribution of the training example.

Step 2: For each training example, do 3 steps 4 steps 5 steps 6 steps 7 steps 8 steps 9 steps 10 steps 11 steps 12.



Fig. 3. The flow chart of ART2+GKA.

Step 3: Update the F1 layer activation.

$$u_1=0 \quad w_1=s_i$$

$$p_i = 0 \quad x_i = \frac{s_i}{e + \|S\|}$$
$$q_i = 0 \quad v_i = f(x_i)$$

- Step 4: Update the F1 layer activation again. Calculate Eqs. (1)–(6).
- Step 5: Calculate the F2 layer activation.

$$y_j = \sum b_{ij} p_i \tag{8}$$

- Step 6: If the reset is true, do steps 7 and 8.
- Step 7: Find the maximum activation unit J in the F2 layer.
- Step 8: Test the vigilance. Calculate Eqs. (1) and (3) and:

$$r_{i} = \frac{u_{i} + cp_{i}}{e + \|U\| + c\|P\|}$$
(9)

If $||r|| < \rho - e$, then $y_J = -1$ and inhibit the unit *J* (return to step 5). If $||r|| \ge \rho - e$, then calculate Eqs. (2), (4), (5) and (6) and do step 9.

Step 9: Do step 10 to 12 N iterations.

c .

Step 10: Update the weight of unit J.

$$t_{Ji} = \alpha du_i + \{1 + \alpha d(d-1)\} t_{Ji},$$

$$b_{iJ} = \alpha du_i + \{1 + \alpha d(d-1)\}b_{iJ}.$$
 (10)

- Step 11: Update the F1 layer activation. Calculate Eqs. (1)–(6).
- Step 12: Test whether the number of stop iterations is reached or not.
- Step 13: Test whether the number of stop epochs is reached or not.

3.2. Genetic K-means algorithm

This study proposes an algorithm, where the main differences between the proposed modified genetic K-means algorithm and the GKA proposed by Krishna and Murty [2002] [9] are as follows:

- 1. It uses the ART2 to find the initial clusters.
- 2. The distance-based mutation is used to escape local solutions and to find the global solution.

 Table 1

 The factors and levels of the proposed experiment

Factors	Levels				
	Ι	II	III		
Clusters	3	5	7		
Dimensions	6	8	10		
Density	Equal	10%	60%		
Error perturbation	Free	Low	High		

 It uses the GKA adopted K-Means Operator (KMO) for faster convergence. However, the KMO in Krishna and Murty's GKA is called one-step K-Means algorithms, so this research focuses on automating the cluster centroids to change one-step KMO.

The GKA coding phase is kept in this research. The offspring is generated based on the best fitness function, distance-based mutation and K-means operator in the population. The GKA procedures are as follows.

3.2.1. Partitional clustering

The main objective of the clustering algorithm under consideration is to partition a collection of ngiven patterns; each pattern is a vector of dimension d, into K groups, such that this partition minimizes the Total Within Cluster Variance (TWCV), which is defined as follows. Let $\{x_{i, i} = 1, 2, ..., n\}$ be the set of n patterns; let x_{ij} denote the *j*th feature of x_i ; define i = 1, 2, ..., n and k = 1, 2, ..., K.

 $W_{ik} = \begin{cases} 1, & \text{if } i\text{th pattern belongs to } k\text{th cluster}, \\ 0, & \text{otherwise} \end{cases}$

Then, the matrix $W=[w_{ij}]$ has the properties that

$$W_{ik} \in \{0, 1\}.$$
, $\sum_{k}^{K} W_{ij} = 1$ (11)

The centroid of cluster k is

$$c_{kj} = \frac{\sum_{i=1}^{n} w_{ik} x_{ij}}{\sum_{i=1}^{n} w_{ik}}$$
(12)



Fig. 4. The 3D figure and corresponding learning curve for each cluster.



Fig. 5. Evolutional process of GKA.

The within-cluster variation of kth cluster is defined as

$$S^{(k)}(W) = \sum_{i=1}^{n} w_{ik} \sum_{j=1}^{d} (x_{ij} - c_{kj})^2$$
(13)

and the TWCV is defined as

$$S(W) = \sum_{k=1}^{K} S^{(k)}(W) = \sum_{k=1}^{K} \sum_{i=1}^{n} w_{ik} \sum_{j=1}^{d} (x_{ij} - c_{kj})^{2}$$
(14)

The objective is to minimize S(W), i.e.,

$$S(W^*) = \min_{W} \{S(W)\}$$
(15)

3.2.2. Coding system [7]

A natural way of coding such *W* into a string, s_w , is to consider a chromosome of length *n* and to allow each allele in the chromosome to take value from $\{1, 2, ..., K\}$. In this case, each allele corresponds to a pattern and its value represents the cluster number to which the corresponding pattern belongs.

3.2.3. Initialize population

The initial population is selected randomly. Each allele in the population can be initialized to a

Table 2

The results of multivariate analysis	s of variance of two methods
--------------------------------------	------------------------------

Factors	ART2+	ART2+
	K-means	GKA
Cluster number	0.000*	0.000*
Dimension	0.736	0.478
Density level	0.297	0.159
Error level	0.000*	0.000*
Cluster number × dimension	0.249	0.721
Cluster number × density level	0.017*	0.984
Cluster number × error level	0.002*	0.000*
Dimension × density level	0.302	0.141
Dimension × error level	0.945	0.907
Density level \times error level	0.219	0.886
Cluster number \times dimension \times density level	0.290	0.136
Cluster number \times dimension \times error level	0.995	0.995
Cluster number \times density level \times error level	0.446	0.998
Dimension × density level × error level	0.733	0.701
Cluster number \times dimension \times density level \times error level	0.839	0.802

*Significant at the 0.05 level.

Table 3					
The average	of misclassifications	under	different	factor (%)	

Factor	Level	ART2+K-means	ART2+GKA
Cluster number	3	0.0744	0.0593
Cluster number	5	0.0253	0.0033
	7	0.0235	0.0036
Dimension	6	0.0460	0.0285
	8	0.0389	0.0175
	10	0.0383	0.0202
Density level	0.1	0.0493	0.0186
	0.5	0.0417	0.0256
	0.6	0.0322	0.0219
Error level	Free	0.0083	0.0024
	Low	0.0215	0.0113
	High	0.0933	0.0525

cluster number randomly selected from the uniform distribution over set $\{1, 2, ..., K\}$. This is avoided by assigning p, the greatest integer which is less than n/K, randomly chosen data points to each cluster and the rest of points to randomly chosen clusters.

3.2.4. Fitness function selection

The selection operator randomly selects a chromosome from the previous population according to the distribution given by

$$P(s_i) = \frac{F(s_i)}{\sum_{i=1}^{N} F(s_i)}$$
(16)

where $F(s_i)$ represents the fitness value of the string s_i in the population, as defined in the next paragraph. This kind of random selection applies to the roulette wheel; however, the string s_w 's fitness function value is based on TWCV. The smaller the S(W), the larger the $f(s_w)$. Furthermore, \overline{f} and σ represent the current population $f(s_w)$'s average and standard error, respectively. In addition, c is a value in [1,3]. $f(s_w)$ and $F(s_w)$ are defined as:

$$f(s_w) = -S(W), \qquad g(s_w) = f(s_w) - (\bar{f} - c\sigma)$$
(17)

$$F(s_w) = \{g(s_w)\}, \text{ if } g(s_w) \ge 0$$
 (18)



Fig. 6. The architecture of the proposed recommendation agent system.

3.2.5. Mutation

Mutation changes an allele value depending on the distances of the cluster centroids from the corresponding data point. To apply the mutation operator to the allele $s_w(i)$ corresponding to pattern X_i , let $d_j = d(X_i, C_j)$ be the Euclidean distance between X_i and C_j (defined as average of *j*th dimension). Then, the allele is replaced

Table 4The hyperlink structure of the PDA Web site

Financ	cial information	n Personal data		Life related information		Sending message	
1	Real-time news	4	Personal	11	Fate	18	Send mail
2	Stock reminder	5	Friends	12	Weather	19	Short Message
3	Currency rate	6	Hyperlink	13	Traffic	20	ICQ
		7	Notes	14	Foodstuffs	21	Leave message
		8	Reminder	15	Emergency		-
		9	Mail manager	16	Video		
		10	Sending-mail recorder	17	News		



Fig. 7. The learning curve with respect to the total distance for ART2.

with a value chosen randomly from the following distribution:

$$p_{j} = P_{r}\{s_{w}(i) = j\} = \frac{c_{m}d_{\max} - d_{j}}{\sum_{i=1}^{K} (c_{m}d_{\max} - d_{i})}$$
(19)

where $c_m \ge 1$ and $d_{\max} = \max_j \{d_j\}$.

3.2.6. K-means operator

3.2.6.1. Initialization. Use random choice for the example *i* (*i*=1, 2..., *m*) and cluster *j* (*j*=1, 2..., *c*), set *j*=1 and *k*=1. (M_j^0 : example assigned to the *j*th cluster, I_j^0 : index of the example assigned the *j*th cluster)

3.2.6.2. Algorithms.

Step 1: Calculate the centroid of cluster *j*.

$$z_j^k = \begin{cases} \frac{1}{M_j^{k-1}} \sum_{i \in I_j^{k-1}} x_i, & \text{if } M_j^{k-1} > 0 \end{cases}$$
(20)

if j = c, then go to step 2, else j = j + 1 and go to step 1.

Step 2: Calculate the distance between each example and centroid.

$$J_1^k = \sum_{j=1}^c \sum_{i \in J_j^{k-1}} \|x_i - z_j^k\|^2$$
(21)

Step 3: Calculate the new assignment, example *i* assigned to the j^* cluster (i.e., $w_{ij^*}=1$, $w_{ij}=0, j=1, \ldots, c; j \neq j^*$)

$$\|x_i - z_{j^*}^k\|^2 \le \|x_i - z_j^k\|^2, \quad j = 1, \dots, c, \ j \ne j^*$$
(22)

If the equal sign is true, then break. If i < m, then redo step 3 and let i=i+1; else all examples are assigned the *j*th cluster and all indices of examples are assigned to the *j*th cluster, go to step 4.

Step 4: Calculate the distance between examples and centroid.

$$J_{2}^{k} = \sum_{j=1}^{c} \sum_{i \in I_{j}^{k-1}} \|x_{i} - z_{j}^{k}\|^{2}$$
(23)

Step 5: If $|J_1^k - J_2^k| < \varepsilon$, then stop, else j=j+1 and k=k+1 go to step 1.

3.3. Integration of ART2 and GKA

Genetic K-means algorithm can find the global optimum, but the initial clusters must be known initially. In this research, the unsupervised neural network ART2 is proposed for deciding the initial cluster for GKA. The flow chart for this is shown in Fig. 3.

3.4. Monte Carlo study

In order to evaluate the efficiency of the clustering methods, the within variance and misclassification rate are calculated for the Monte Carlo simulation

Table 5
The within cluster variations of ART2 + K-means and ART2 + GKA

	Mean within cluster variance
K-means	1141.7
ART2	851.2
ART2+K-means	647.8
SOM+K-means	650.1
ART2+GKA	592.95
SOM+GKA	592.95

data. There are several factors which can affect the quality of the solution:

- 1. the number of clusters,
- 2. the number of dimensions,
- 3. density: the different degree of scatter of the data point, and
- 4. error perturbation to simulate the error of data collection or measurement.

The factors and levels of this experiment are shown in Table 1, and the result is a $3 \times 3 \times 3 \times 3$ full factorial design with three replications. Totally, there are 243 data sets and each set contains 120 data points.

3.5. Hypothesis testing

The number of misclassifications of two clustering methods is compared with respect to sensitivity and robustness of the two clustering methods. A misclassification is indicated that supposes D point belonging to the second cluster generated by the simulation algorithm, but D point is clustered to the first cluster by ART2+K-means. A misclassification is recorded to ART2+K-means. There are five hypotheses for evaluating the performance of two clustering methods.

Hypothesis 1. The number of misclassification does not differ across the levels of clusters.

Hypothesis 2. The number of misclassifications does not differ across the levels of dimensions.

Hypothesis 3. The number of misclassifications does not differ across the levels of density.

Hypothesis 4. The number of misclassifications does not differ across the levels of error perturbation.

Hypothesis 5. The number of misclassifications does not differ across the two clustering methods.

4. Simulation

4.1. Verification of random number generator

The simulation data sets were implemented (described in Section 3.1) in order to verify the efficiency of the two clustering tools. The random number generator must correspond to normal and uniform distribution. Firstly, 1000 data points were generated via the random number generator, which grouped them into 20 segments. The chi-square test showed that these data fit the normal and uniform distribution.

The testing results show that the random numbers generated by the generator fit a normal and uniform distribution. Thus, it is reasonable to accept the reliability of the random number generator.

4.2. Simulation data sets generation

The three phases of writing the simulation program are as follows. Each phase generates 81 data sets and



Fig. 8. The learning curves of ART2+K-means and ART2+GKA.



(a) The three dimensions space data of ART2+GKA

Fig. 9. The results of ART2 + GKA and SOM + GKA. (a) The three dimensions space data of ART2 + GKA. (b) The topological space of SOM + GKA.

2

~4 ~ 1²¹²

6

+Data

Table 6 The frequency statistics table of ART2+GKA

	262					
	203	303	375	366	359	209
%)	45	37	51	33	34	47
(%)	55	63	49	67	66	53
20 (%)	40	45	55	50	11	7
(%)	45	40	40	44	44	45
(%)	18	15	5	6	45	47
: (%)	69	63	66	69	17	20
ss (%)	9	10	13	11	43	45
%)	12	9	6	7	12	8
(%)	10	18	15	13	22	27
senior	7	8	7	6	9	5
hool (%)						
e or	78	81	83	77	75	70
ity (%)						
raduate	15	11	10	17	16	35
	%) (%) 20 (%) (%) (%) t (%) sss (%) (%) (%) (%) senior hool (%) c or ity (%) raduate (%)	$\langle \gamma_0 \rangle$ 45 $\langle \langle \gamma_0 \rangle$ 55 20 ($\langle \gamma_0 \rangle$) 40 $\langle \langle \gamma_0 \rangle$ 45 $\langle \langle \gamma_0 \rangle$ 18 t ($\langle \gamma_0 \rangle$) 69 sss ($\langle \gamma_0 \rangle$) 12 $\langle \langle \gamma_0 \rangle$ 10 senior 7 hool ($\langle \gamma_0 \rangle$) 2 z or 78 ity ($\langle \gamma_0 \rangle$) 15 ($\langle \gamma_0 \rangle$) 15	7_0 45 37 (9_0) 55 63 20 40 45 (9_0) 40 45 (9_0) 45 40 (9_0) 18 15 t (9_0) 69 63 ss (9_0) 9 10 (9_0) 12 9 (9_0) 10 18 senior 7 8 hool (9_0) 2 9 c or 78 81 ity (9_0) 15 11 (9_0) 15 11	7_0 45 57 51 (9_0) 55 63 49 20 (%) 40 45 55 (9_0) 45 40 40 (9_0) 18 15 5 (9_0) 18 15 5 $t(9_0)$ 69 63 66 (9_0) 12 9 6 (9_0) 10 18 15 senior 7 8 7 hool (%)	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	(%) 45 37 51 33 34 $(%)$ 55 63 49 67 66 20 $(%)$ 40 45 55 50 11 $(%)$ 45 40 40 44 44 $(%)$ 18 15 5 6 45 t $(%)$ 69 63 66 69 17 ss $(%)$ 9 10 13 11 43 $(%)$ 12 9 6 7 12 $(%)$ 10 18 15 13 22 senior 7 8 7 6 9 hool (%)

replicates three times. The total number of data sets is 243.

Phase 1: Generate the error-free data sets.

Phase 2: Generate the low-error data sets.

Phase 3: Generate the high-error data sets.

4.3. Experimental results and analysis

4.3.1. Results of ART2

The values of parameters in Section 3.2.2 and the total distance (TD) used to evaluate the convergence of ART2 can be shown as:

$$TD = d(1-d) \sum_{i=1}^{P} \sum_{j=1}^{M} \left[\frac{u_i}{1-d} - t_{ji} \right]$$
(24)

where *d* is defined in Eq. (7), *P* is the number of training patterns, *M* is the number of output units and t_{ji} is the top to down weights of the activation unit for every training pattern. If TD decreases gradually, it is said that ART2 can converge well. Fig. 4 illustrates the learning curve and presents the data set in three-dimensional (3D) space (*Z* data shows the number of data points).

4.3.2. Results of GKA

The data set of three clusters, six dimensions, 0.1 density condition and high-error is taken as an example and shown in Fig. 5.

4.3.3. Comparison of two clustering methods

To examine the performance of two clustering methods, the multivariate analysis of variance test (MANOVA) is used to test the results of the different factors shown in Table 2 and the average misclassifications under different factors are shown in Table 3. The main effect of each factor is discussed in this research. According to the results in Tables 2 and 3, there is further discussion as follows.

Hypothesis 1. The number of misclassification does not differ across the levels of clusters.

Table 2 shows that the number of clusters affects the cluster recovery of two methods at 0.05 significance level and Table 3 shows that the cluster recovery becomes better for each method.

Hypothesis 2. The number of misclassifications does not differ across the levels of dimensions.

The number of dimensions does not affect the cluster recovery of two methods according to Table 2. As the number of dimensions increases, ART2 + K-means will increase the accuracy of clustering but ART2 + GKA will not, as shown by Table 3.

Hypothesis 3. The number of misclassifications does not differ across the levels of density.

According to Table 2, the density levels do not affect two cluster tools. Table 3 shows that ART2+K-means has better accuracy under high density.

Hypothesis 4. The number of misclassifications does not differ across the levels of error perturbation.

Table 2 shows the error perturbation effects of two methods. The mean misclassifications of two methods increase for the error free, low error and high error data sets, respectively.

 Table 7

 Browsing path categories for each cluster

Cluster	Path categories
1	Personal Data, Sending Message
2	Life-related information, Sending Message
3	Personal Data, Life-related information, Sending Message
4	Personal Data, Life-related information
5	Financial Information, Life-related information
6	Financial Information, Personal Data, Sending Message

Hypothesis 5. The number of misclassifications does not differ across the two clustering methods.

In order to test whether or not the two clustering tools have significant differences, Scheffe's multiple comparison tests used. The *p*-value shows that the two cluster methods do not differ significantly. However, the average of within cluster variance of ART2 + GKA, 48,020, is less then that of ART2 + K-means, 53,629. The ART2 + GKA uses the fitness function [Eq. (18)] to find the optimal solution and decrease the within cluster variance.

5. Model evaluation results and discussion

The proposed method, ART2+GKA, is excellent for clustering analysis, as shown in Section 4. To further document the proposed method, an advanced comparison of the two methods was made using real data being collected from a Web PDA company. By employing the proposed method, this research also develops a recommendation agent system for the endusers, or customers. The system is able to find the user scope in the same cluster and then use a feedforward neural network with back-propagation learning algorithm (BPN) to classify new users. The system can dramatically increase customer satisfaction using the proposed method. The following sections present the system analysis, data preprocessing, clustering analysis and the recommendation agent system.

5.1. The system analysis

There are three phases for the proposed agent system, data preprocessing, data mining and recommendation agent developing processes. The first phase, data preprocessing, is the mechanism for collecting the browsing paths of client user and storing these paths in the Web database. Analyzing the browsing paths in the Web database is implemented for the second phase, data mining, using the proposed clustering method, ART2+GKA, and the clustering results are stored in the clustering database. Finally, the third phase, recommendation agent developing, develops a recommendation agent system to analyze the user scope



Fig. 10. The different browsing preferences.

from the clustering database and recommend Web pages to previous login users. If the user is a new member, the agent will use a BPN to determine to which cluster he/she belongs. Fig. 6 demonstrates the architecture of the proposed recommendation agent system.

5.2. Data preprocessing

The browsing paths of a Web PDA company were collected for analysis. This company has 1875 members, and their browsing path data was collected from September 2000 to January 2001. The hyperlink structure of the Web site is illustrated in Table 4. Totally, there are 21 hyperlinks, which can be classified into the four categories of finance, personality, life and message. In order to analyze the browsing paths with ART2, the data were transformed into a matrix. The browsing page is set to 1 if the customer clicked the hyperlink of the browsing page and set to 0 if the customer did not

click the hyperlink. After transforming, 1875 data sets were selected, which served as the training patterns of ART2.

5.3. Clustering analysis

In addition to the proposed method, ART2 + GKA, ART2 neural network followed by K-means (ART2 + K-means) was also applied for comparison with the proposed method. Here, 21 hyperlinks were the input patterns for ART2 neural network, and the parameter vigilance was set to 0.6. The learning curve and total distance are shown in Fig. 7, including that the ART2 neural network can converge very fast. After training, there are six output nodes, after which, the ART2 neural network result is forwarded to GKA and K-means. Not only the number of clusters but also the starting points are input to GKA and K-means. This means that the browsing path data for 1875 members are clustered into six segments. In the current case study, after determining



Fig. 11. The user scope. The scope will recommend and present when the user logs in next time.

the number of clusters, six, and starting points, they are all forwarded to both K-means and GKA as the initial solution. The within-cluster variations of ART2+K-means, ART2+GKA, K-means, ART2, SOM+K-means and SOM+GKA [10,11] [Kuo, 2002c] are shown in Table 5. The within-cluster variations of ART2+K-means and ART2+GKA are 647.8 and 592.95, respectively, which is a 9.25% decrease. Fig. 8 illustrates the mean withincluster variations for both of these methods and others. The clustering precision of ART2+GKA is better than that of ART2+K-means in this study, similar to the results that obtained in Section 2. Fig. 9 shows the data, ART2+GKA, presented in the threedimensional space and topological space of SOM+GKA. To determine the number of clusters of SOM+GKA is more difficult than ART2+GKA. Table 6 displays the percent ages of sex, age, occupation and education each cluster, and Table 7 shows the browsing path of categories. Fig. 10 shows that different browsing preferences exist in different clusters. The browsing path numbers can be found in Table 4.

5.4. Implementation of recommendation agent

After the data preprocessing and data mining through ART2+GKA, six clusters are found to have different browsing preferences. The customers in the same cluster have the same preferences, but the user scope may not be the same. The recommendation agent will analyze the user scope in one cluster. In Fig. 11, if the cluster member (1624) has the different cluster scope, then the recommendation agent will recommend and present the Web page to member 1624 when he/she logs in next time.

The home page of the PDA Web site is shown in Fig. 12. If the user is a member and logs into the Web site, the recommendation agent will search the user attributes in the cluster's database and recommend



Fig. 12. The home page of the PDA Web site.

pages of the cluster scope. The recommendation mechanism is shown in Fig. 13.

From the above, only an old member can be classified to exact cluster. However, if a new user logs in to the system, the system is not able to determine his/her preferences. Thus, BPN is applied to learn the above clustering results. Once a new user logs on to the system, it can classify the new user and find out his/her preferences. The architecture of BPN includes three layers.

The first layer is the input layer with 21 hyperlinks input vectors. The decision of hidden layer nodes do not have the perfect equations or model recently; therefore, the number of hidden layer nodes is set to 35, 40 and 50 for this experiment. The output layer has six nodes so that the result shows the cluster of new user. In addition to the hidden layer nodes, the momentum and learning rate are set to three different levels, say 0.2, 0.4 and 0.6. For the 1875 patterns, they are divided into training patterns and testing patterns. Their amounts are 1500 and 375, respectively. For each factor and level, both the mean square error (MSE) and misclassification rate (MR) are calculated. The MSE is represented as:

$$MSE = \sqrt{\frac{\sum_{p}^{M} \sum_{j}^{N} (T_{j}^{p} - Y_{j}^{p})^{2}}{MN}}$$
(25)

where T_j^p is the actual output of *j*th output node for *p*th pattern, Y_j^p is the network output of *j*th output nodes for *p*th pattern, *M* is the number of training patterns, and *N* is the number of output layer nodes. The MR is represented as:

$$MR = \frac{Number of misclassification patterns}{Total patterns}$$
(26)



Fig. 13. The recommendation mechanism.



Fig. 14. The learning curve of training and testing data after 1000 epochs.

This result shows that when the number of hidden layer nodes is 50, the learning rate is 0.2 and the momentum is 0.4, then the MSE is the lowest. Fig. 14 shows the convergence of training and testing data in BPN. This network is used to develop the classification system. One example of the classification results for a new user is shown in Fig. 15.

6. Conclusions

In a clustering problem, it is always difficult to determine the number of clusters. Therefore, this study proposes a two-stage method, which first uses the Adaptive Resonance Theory 2 (ART2) to determine the number of clusters and an initial solution, then using genetic K-means algorithm (GKA) to find the final solution. Sometimes, the self-organizing feature map with two-dimensional output topology has great difficulty determining the number of clusters by observing the map. However, ART2 can actually determine the number of clusters according to the number of output nodes. Through Monte Carlo simulation and a real case problem, the proposed two-stage clustering analysis method, ART2+GKA, has been shown to provide high performance. The *p*-value of Scheffe's multiple comparison test shows that the two cluster methods, ART2+K-means and ART2+GKA, do not differ significantly, but the average of within cluster variance of ART2+GKA is less than that of ART2+K-means. This may be because ART2+GKA has the characteristics of both a genetic algorithm and K-means.

In the real-world case study, the browsing paths of a Web PDA company were clustered by both ART2+K-means and ART2+GKA. The results from



Fig. 15. The classification of new user.

ART2 + GKA are much better than those of ART2 + K-means, demonstrating that ART + GKA is an efficient tool for clustering analysis. Based on the clustering result, the Web administrators can make more effective Webs for the customers. After understanding the customers' behaviors, the recommendation mechanism can be more easily and precisely created. Because customers in the same cluster have similar characteristics, this mechanism can recommend Web pages that are clicked more frequently for the same cluster. Thus, for a larger Web site, this process may save search time, thus increasing the customers' convenience and satisfaction.

Future research can improve the current study. For instance, the parameters of GKA, like the crossover and mutation rates, affect the time to converge, so an experimental design can decide the best parameter combination to speed up the convergence. Because an ant colony system is also effective at searching, it may be a good candidate for replacing the ART2 neural network.

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