

Complement Coding Example

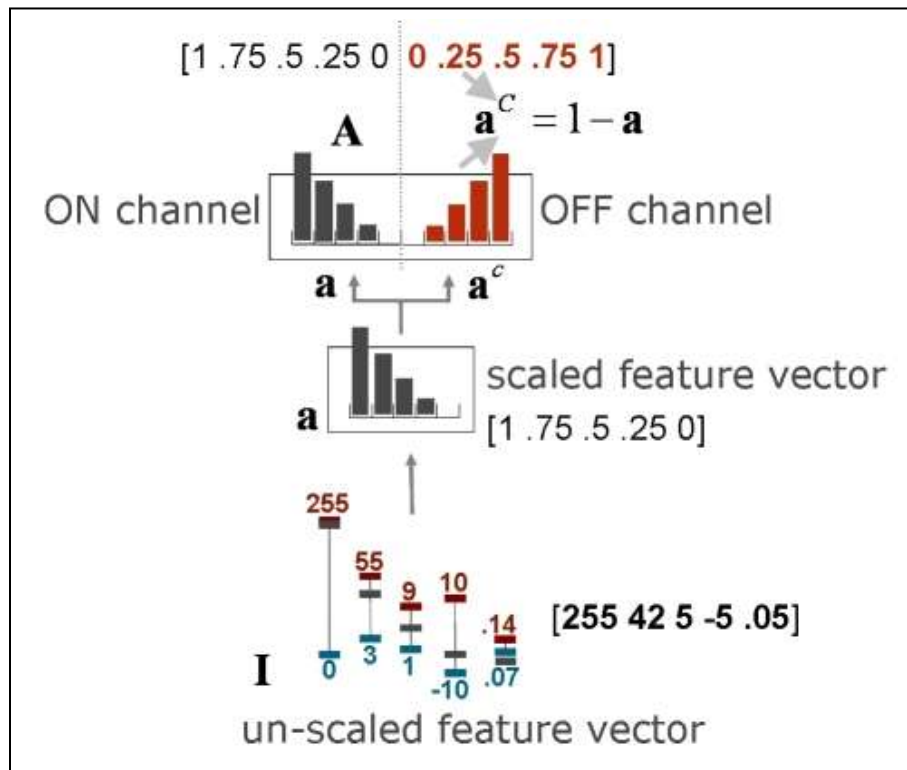
Usage: `Complement_Code(feet_vect,min_vect,max_vect) :`

feat_vect is an input feature vector of size $1 \times M$ where M is the number of features.

min_vect is a row vector of size $1 \times M$ indicating the *minimum* allowable feature values.

max_vect is a row vector of size $1 \times M$ indicating the *maximum* allowable feature values.

The following example is depicted in this complement coding icon



Consider an un-scaled, five-dimensional input feature vector $I = [255 \ 42 \ 5 \ -5 \ 0.05]$, where each feature has the following pair of *minimum* and *maximum* allowable values:

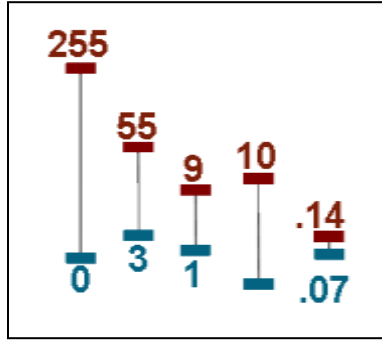
$$I_1^{\min} = 0 \quad I_1^{\max} = 255$$

$$I_2^{\min} = 3 \quad I_2^{\max} = 55$$

$$I_3^{\min} = 1 \quad I_3^{\max} = 9$$

$$I_4^{\min} = -10 \quad I_4^{\max} = 10$$

$$I_5^{\min} = 0.07 \quad I_5^{\max} = 0.14$$



The minimum and maximum values are depicted as shown above.

The **min_vect** and **max_vect** feature values, based on the above values, are:

$$\mathbf{min_vect} = [0 \ 3 \ 1 \ -10 \ 0.07]$$

$$\mathbf{max_vect} = [255 \ 55 \ 8 \ 10 \ 0.14]$$

The complement coded feature vector is obtained by running:

Complement_Code(feet_vect,min_vect,max_vect)

$$\equiv \mathbf{Complement_Code}([255 \ 42 \ 5 \ -5 \ 0.05], [0 \ 3 \ 1 \ -10 \ 0.07], [255 \ 55 \ 9 \ 10 \ 0.14])$$

To give the 10-dimensional complement coded output:

$$[1.0 \ .75 \ .50 \ .25 \ 0 \ 0 \ .25 \ .50 \ .75 \ 1.0]$$

Each feature value is first scaled into the [0 1] range by using the minimum and maximum feature values, and all values that exceed the maximum or are below the minimum are truncated to 1 and 0 respectively.

$$\text{Therefore, } a_2 = (I_2 - \text{minimum}) / (\text{maximum} - \text{minimum}) \equiv (42 - 3) / (55 - 5) = 0.75$$

In the case of feature I_5 , the feature value is less than the allowable minimum $I_5^{\min} = 0.07$.

As a result, a_5 is truncated to 0.

Also, each feature and its complement in the complement coded vector add up to 1.

$$a_1 + a_6 \equiv 1 + 0 = 1$$

$$a_2 + a_7 \equiv 0.75 + 0.25 = 1$$

$$a_3 + a_8 \equiv 0.50 + 0.50 = 1$$

$$a_4 + a_9 \equiv 0.25 + 0.75 = 1$$

$$a_5 + a_{10} \equiv 0 + 1 = 1$$

Batch mode:

In the batch mode, multiple feature vectors, I , are provided in a single array with each row being one un-scaled feature vector.

To complement code un-scaled feature vectors I^a , I^b , and I^c , where the vectors are:

$$I^a = [255 \ 42 \ 5 \ -5 \ 0.05]$$

$$I^b = [102 \ 29 \ 7 \ -4 \ 0.14]$$

Using the same minimum and maximum feature values as above, the complement coded feature vectors can be obtained in an array by running

Complement_Code(data , min_vect, max_vect) \equiv

Complement_Code ([255 42 5 -5 0.05; 102 29 7 -4 0.14],
[0 3 1 -10 .07],
[255 55 9 10 0.14])

The output is as follows:

```
[ 1.0 .75 .50 .25 0.0 0.0 .25 .50 .75 1.0
  0.4 .50 .75 .30 1.0 0.6 .50 .25 .70 0.0 ]
```

The rows in the output array correspond to the complement coded vector of I^a and I^b .

When running the code with the same input data, but without the *minimum* and *maximum* vectors, the *minimum* and *maximum* values are imputed from the data.